

# Towards Metrics and Visualizations Sensitive to Coevolutionary Failures

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AAAI 2005 Fall Symposium:  
Coevolutionary and Coadaptive Systems



# Outline

- 1 Motivation
  - Introduction
  - Best-of-Generation (BOG) Techniques
- 2 Techniques
  - All-of-Generation (AOG) Techniques
  - Population-Differential Metric
- 3 Observations & Results
  - Profiles: Coevolutionary Successes & Failures
  - Examples: Coevolutionary Successes & Failures

# Motivation

## Coevolutionary Fitness

- No objective fitness function **required**

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- How to best **monitor** performance?

# Notation

From (Bucci & Pollack)

- **Candidate** population  $C$ , **Test** population  $T$

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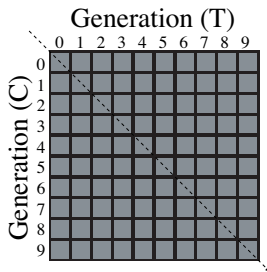


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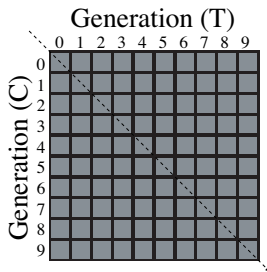
- **Candidate** population  $C$ , **Test** population  $T$
- Any candidate can be **evaluated** against any test.
- Outcome is an element of some ordered set  $R$   
 $R = \{CandidateFailedTest < CandidateTiedTest < CandidatePassedTest\}$

# Generation-Table Analysis



- **CIAO data** (Cliff and Miller)

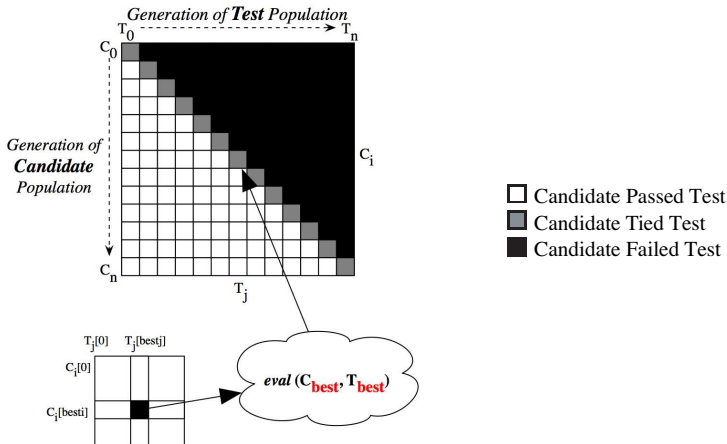
# Generation-Table Analysis



- **CIAO data** (Cliff and Miller)
- **Dominance Tournament** (Stanley and Miikkulainen)
- **Master Tournament** (Nolfi and Floreano)
- **Hall-of-Fame** (Rosin and Belew)

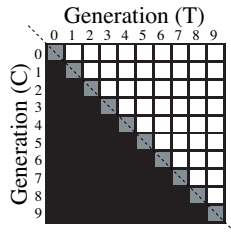
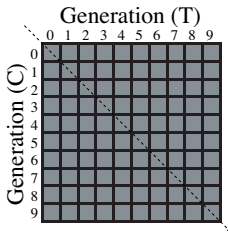
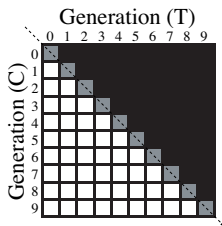
# Best-of-Generation (BOG) Approach

## Evaluation



# "Instantaneous Fitness"

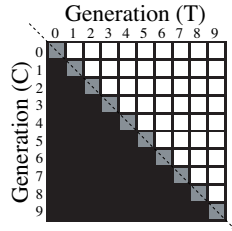
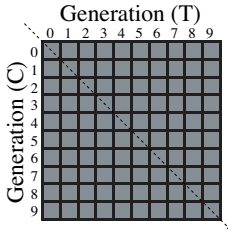
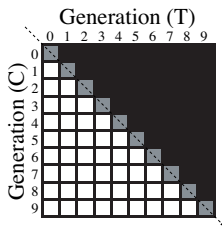
## "Red Queen" Dynamics



- Candidate Passed Test
- Candidate Tied Test
- Candidate Failed Test

# "Instantaneous Fitness"

"Red Queen" Dynamics



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Simulations may drastically differ, yet may generate identical "instantaneous fitness" profiles

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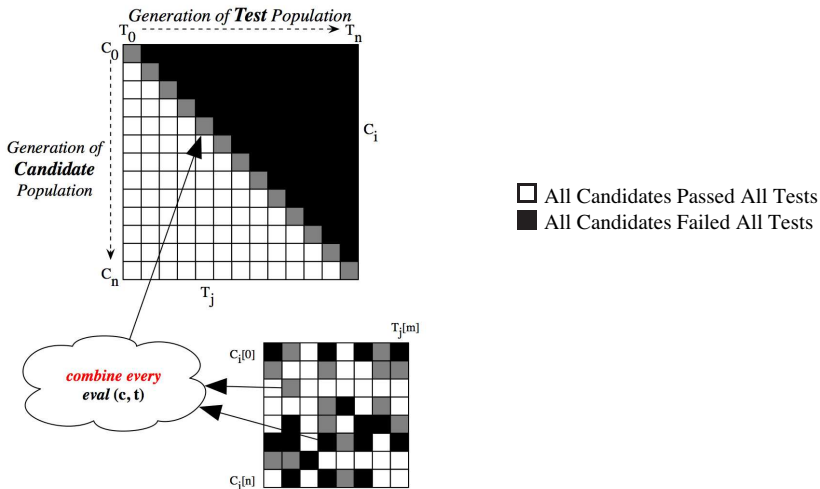
# Best-of-Generation (BOG) Approach

- Low computational cost
- Definition of "best" is pre-defined
- Only reflects behavior of "best" individuals
- High sensitivity to coevolutionary success  
**Low sensitivity to coevolutionary failure**

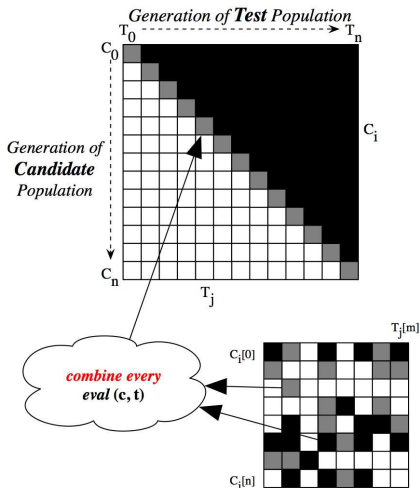
# Best-of-Generation (BOG) Approach

- Low computational cost
- Definition of "best" is pre-defined
- Only reflects behavior of "best" individuals
- High sensitivity to coevolutionary success  
**Low sensitivity to coevolutionary failure**
- Not appropriate for examining failures in coevolution.  
All-of-Generation (AOG) based analysis is a response...

# All-of-Generation: Population-Grained Evaluation



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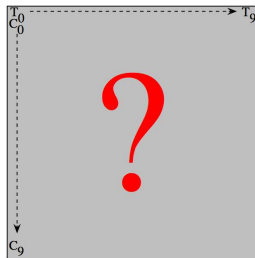
- All Candidates Passed All Tests
- All Candidates Failed All Tests

Here: simple average  
of outcome values

# BOG vs. AOG Differentiating Example

0	1	2	3	4	5	6	7	8	9
0	-1	-2	-3	-4	-5	-6	-7	-8	-9
0	-1	-2	-3	-4	-5	-6	-7	-8	-9
0	-1	-2	-3	-4	-5	-6	-7	-8	-9
0	-1	-2	-3	-4	-5	-6	-7	-8	-9
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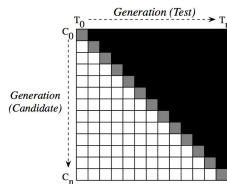
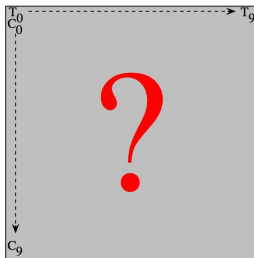
0	0	0	0	0	0	0	0	0	0
1	-1	-1	-1	-1	-1	-1	-1	-1	-1
2	-2	-2	-2	-2	-2	-2	-2	-2	-2
3	-3	-3	-3	-3	-3	-3	-3	-3	-3
4	-4	-4	-4	-4	-4	-4	-4	-4	-4
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7	-7	-7	-7	-7	-7	-7	-7	-7	-7
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0	0	0	0	0	0	0	0	0	0
1	-1	-1	-1	-1	-1	-1	-1	-1	-1
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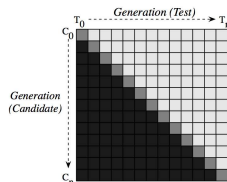
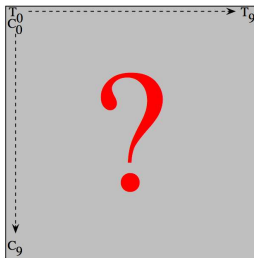


**BOG table:**  
**a success!**

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3	-1	-2	-3	-4	-5	-6	-7	-8	-9	
4	-1	-2	-3	-4	-5	-6	-7	-8	-9	
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6	-1	-2	-3	-4	-5	-6	-7	-8	-9	
7	-1	-2	-3	-4	-5	-6	-7	-8	-9	
8	-1	-2	-3	-4	-5	-6	-7	-8	-9	
9	-1	-2	-3	-4	-5	-6	-7	-8	-9	

0	0	0	0	0	0	0	0	0	0	0
1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2
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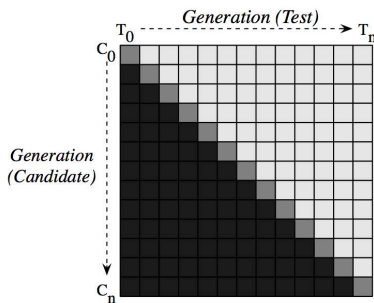
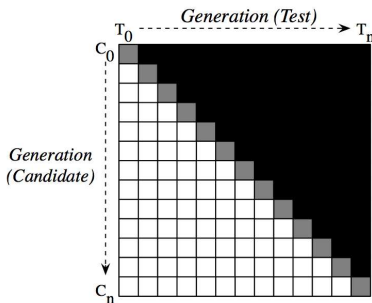


AOG table:  
a failure



# BOG vs. AOG Differentiating Example

Which is preferable?



- All Candidates Passed All Tests
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# The Population-Differential Metric

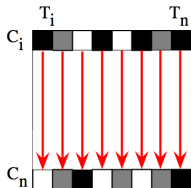
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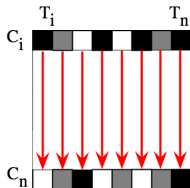
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- **"Compare-on-one" variant**: Individuals are points on 2D grid. The "winner" has the higher value in test's greater dimension.

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Sought to reproduce common coevolutionary behaviors:

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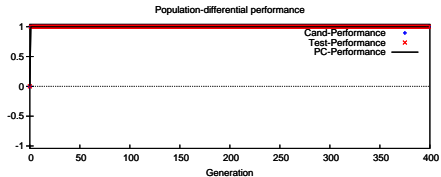
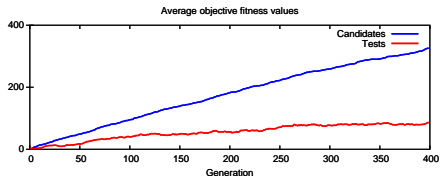
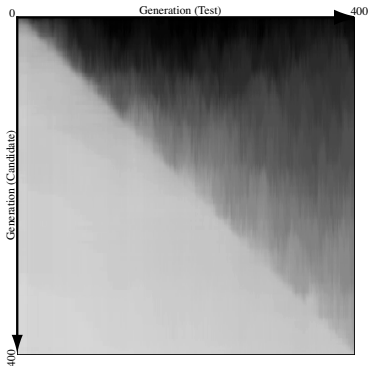
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Sought to reproduce common coevolutionary behaviors:

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- "variation"
- "disengagement" (due to lack of gradient)
- "cycling"

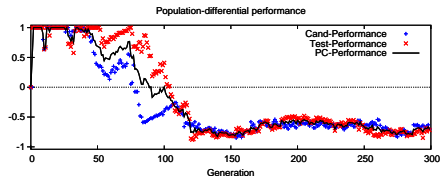
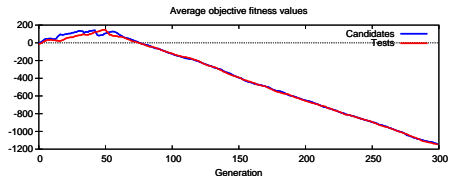
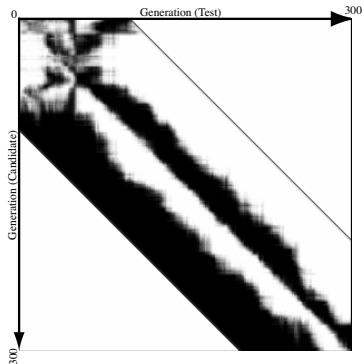


# Behavior Example: Arms-Race Dynamics



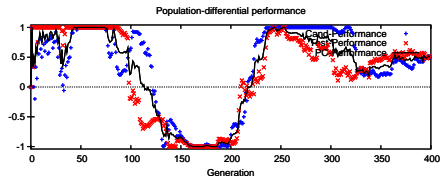
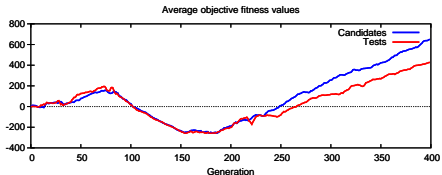
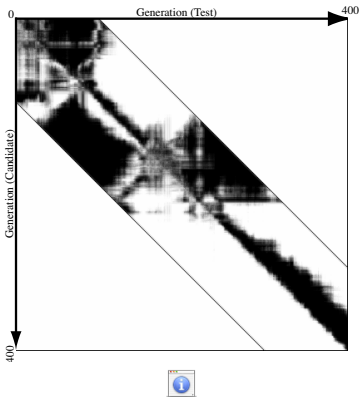


# Behavior Example: Lock-In Failure

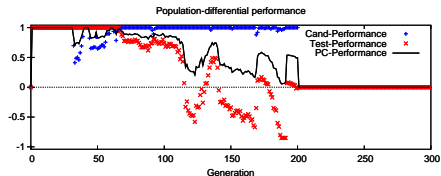
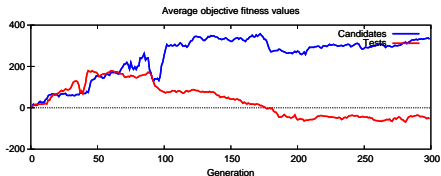
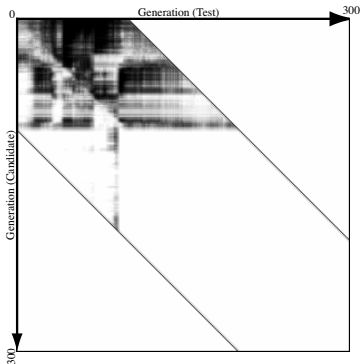




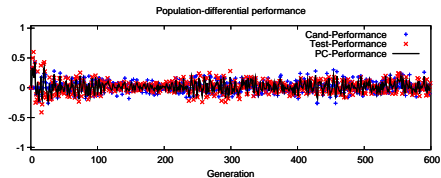
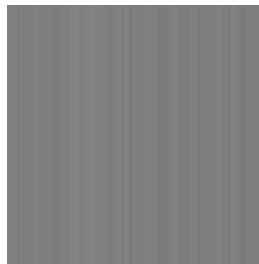
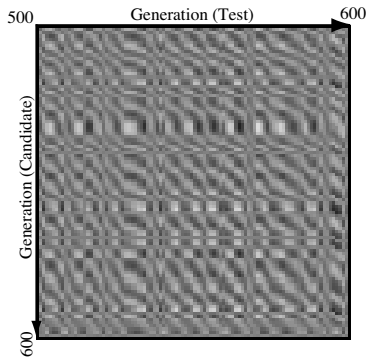
# Behavior Example: Variation



# Behavior Example: Disengagement



# Behavior Example: Cycling



# Summary

- BOG-based analysis is good for monitoring successes but not so good for monitoring failures
- AOG-based analysis uses information on the entire population (not just the "best")
- The "Generation-Table approach" to coevolutionary analysis continues to yield useful techniques.

# Thank you

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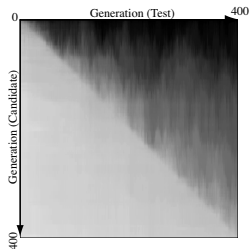
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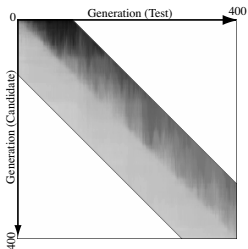


# AOG Memory Policies to Reduce Computation

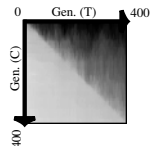
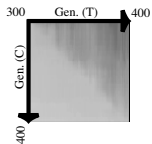
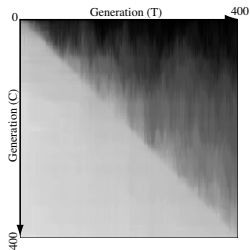
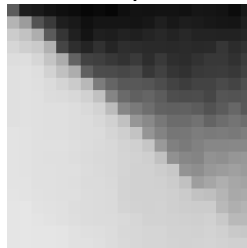
## Lossless



## Bounded



## Sampled



# Memory Size Can Affect Interpretation

